PIPES PROBLEMS SOLUTIONS

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Pipes & Cisterns

Inlet Pipe: A pipe used to fill the tank or cistern is known as Inlet Pipe.

Outlet Pipe: A pipe used to empty the tank or cistern is known as Outlet Pipe.

Basic Rules

If an inlet pipe takes 2 hours to fill a tank then it will fill ½ of the tank per hour If an outlet pipe can empty the tank in 4 hours then it will empty \(\frac{1}{4} \) of the tank per hour If both of the above inlet and outlet pipes are opened at once then it will fill the tank \(\frac{1}{2}\) $-\frac{1}{4} = \frac{1}{2}$ of the tank per hour

Example 1:

A tank can be filled by a tap in 20 minutes and by another tap in 60 minutes. Both the taps are kept open for 10 minutes and then the first tap is shut off. After this, the tank will be completely filled in:

Solution:

Part filled in 10 min. =
$$10 \left[\frac{1}{20} \right] + \left[\frac{1}{60} \right] = 10 \times \frac{4}{60} = \frac{2}{3}$$

Remaining part = $1 - \frac{2}{3} = \frac{1}{3}$
Part filled by second tap in 1 min. = $\frac{1}{60}$

$$\frac{1}{60} : \frac{1}{3} : : 1 : x$$

Hence, the remaining part will be filled in 20 min.

Example 2:

A cistern can be filled in 9 hours but it takes 10 hours due to in its bottom. If the cistern is full, then the time that the leak will take to empty it, is:

Solution:

Work done by the leak in 1 hour =
$$\frac{1}{9} - \frac{1}{10} = \frac{1}{90}$$

Leak will empty the full cistern in 90 hours.

Exercise

- 1) Pipe A can fill a tank in 5 hours, pipe B in 10 hours and pipe C in 30 hours. If all the pipes are open, in how many hours will the tank be filled?
 - a) 2

d) 3.5

e) None of these

2)	A pump can fill a tank with water in 2 hours. Because of a leak, it took $2x1/3$ hours to fill the tank. The leak can drain all the water of the tank in			
	a) 5 Hours	b) 7 Hours	c) 8 Hours	
	d) 14 Hours	e) None of these	,	
3)	* *	k in 20 and 24 minutes respective nute. All the three pipes working ty of the tank is	• • • • • • • • • • • • • • • • • • • •	
	a) 60 gallonsd) 180 gallons	b) 80 gallons e) None of these	c) 120 gallons	
4)	Two pipes can fill a tank in 10 hours and 12 hours respectively while a third pipe empties the full tank in 20 hours. If all the three pipes operate simultaneously, in how much time will the tank be filled?			
	a) 7 hrs 30 min	b) 7 hrs 45 min	c) 8 hrs 30 min	
	d) 8 hrs 45 min	e) None of these		
5)	A leak in the bottom of a tank can empty the full tank in 8 hours. An inlet pi water at the rate of 6 litres a minute. When the tank is full, the inlet is open due to the leak, the tank is empty in 12 hours. How many litres does the hold?			
	a) 7580	b) 7960	c) 8290	
	d) 8640	e) None of these	,	
6)	taps are open then due t	fill a tank in 5 hours and 20 hours to a leakage, it took 30 minutes not ill it take for the leakage alone to b) 9 hrs e) None of these	nore to fill the tank. If the	
7) Two pipes A and B can fill a tank in 20 and 30 minutes respipes are used together, then how long will it take to fill the		the tank?		
	a) 12 min	b) 15 min	c) 25 min	
	d) 50 min	e) None of these		
8)	12 hours. If all the three	ly. Pipe C can empty it in the tank will be filled in c) $3 \times \frac{9}{17}$ hours		
	$\frac{17}{17}$ moders	$\frac{1}{11}$ Hours	$\frac{17}{17}$ Hours	
	a) $1 \times \frac{13}{17}$ hours d) $4 \times \frac{1}{2}$ hours	e) None of these		
9)		l a tank when the capacity of eaceded to fill the same tank, if the		

c) 16

b) 15 e) None of these

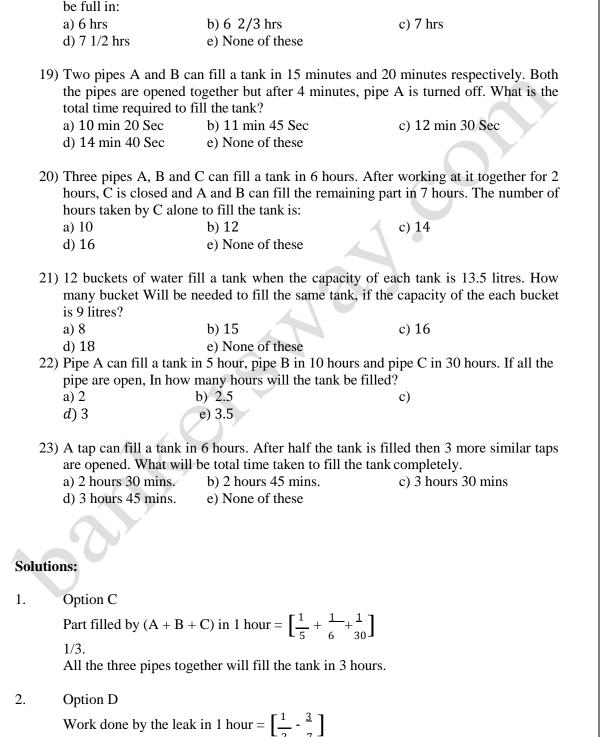
a) 8

d) 18

10)	respectively. There is a three pipes are simultar	can separately fill a cistern in the third pipe in the bottom of the neously opened, then the cistern be alone can empty the cistern? b) 100 min e) None of these	cistern to empty it. If all the	
11)	A cistern can be filled by a tap in 4 hours while it can be emptied by another tap in 6 hours. If both the taps are opened simultaneously, then after how much time will he cistern get filled?			
	a) 4.5 Hours d) 7.2 Hours	b) 5 Hourse) None of these	c) 6.5 Hours	
12)	respectively. How many	lled by two pipes A and B in 60 y minutes will it take to fill the take and A and B fill it together for tb) 20 min e) None of these	anker from empty state if B	
13)	3) One pipe can fill a tank three times as fast as another pipe. If together the two pipe can fill the tank in 86 minutes, then the slower pipe alone will be able to fill the tain			
	a) 81 min d) 192 min	b) 108 min e) None of these	c) 144 min	
14)	4) A tap can fill a tank in 6 hours. After half the tank is filled, three more similar taps are opened. What is the total time taken to fill the tank completely? a) 3 hrs 15 min b) 3 hrs 45 min c) 4 hrs d) 4 hrs 15 mins e) None of these			
15)	Two pipes A and B can fill a tank in 6 hours and 4 hours respectively. If they are opened on alternate hours and if pipe A is opened first, in how many hours, the tank shall be full?			
	a) 4 Hrs d) 9 Hrs	b) 5 Hrs e) None of these	c) 7 Hrs	
16)	Two pipes A and B can fill a cistern in $37\frac{1}{2}$ minutes and 45 minutes respectively. Both pipes are opened. The cistern will be filled in just half an hour, if the B is turned off after:			
	a) 5 d) 15	b) 9 e) None of these	c) 10	
17)	7) A tank is filled in 5 hours by three pipes A, B and C. The pipe C is twice as fast as B and B is twice as fast as A. How much time will pipe A alone take to fill the tank			
	a) 20 hours	b) 25hours	c) 35 hours	

e) None of these

d) Data inadequate



18) Three taps A, B and C can fill a tank in 12, 15 and 20 hours respectively. If A is open all the time and B and C are open for one hour each alternately, the tank will

1/14

Leak will empty the tank in 14 hours.

3. Option C

Work done by the waste pipe in 1 minute $=\frac{1}{15} - \left[\frac{1}{20} + \frac{1}{24}\right] = \left[\frac{1}{15} - \frac{11}{20}\right] = -\frac{1}{40}$ (-ve sign means emptying) volume of 1/40 part = 3 gallons. Volume of whole = (3×40) = 120 gallons.

4. Option A

Net apart filled in 1 hour = $\begin{bmatrix} \frac{1}{4} + \frac{1}{4} - \frac{1}{4} \end{bmatrix} = \frac{8}{60} = \frac{2}{15}$. Therefore the tank will be full in $\frac{15}{2}$ hours = 7 hours 30 minute

5. Option D

Work done by the inlet in 1 hour = $\left[\frac{1}{8} - \frac{1}{12}\right] = \frac{1}{24}$ Work done by the inlet in 1 minute = $\left[\frac{1}{24} \times \frac{1}{60}\right] = \frac{1}{1440}$ Volume of $\frac{1}{1440}$ part = 6 litres. Therefore, Volume of whole = $\left[1440 \times 6\right]$ = 8640 litres

6. Option D

Part filled by (A + B) in 1 hour =
$$\left[\frac{1}{5} + \frac{1}{20}\right]$$

= $\frac{1}{4}$

So, A and B together can fill the tank in 4 hours. Work done by the leak in 1 hour = $\left[\frac{1}{4} - \frac{2}{9}\right] = \frac{1}{36}$ Therefore, leak will empty the tank in 36 hours.

7. Option A

Part filled by A in 1 min.
$$= \frac{1}{20}$$
Part filled by B in 1 min.
$$= \frac{1}{30}$$
Part filled by (A + B) in 1 min.
$$= \left[\frac{1}{20} + \frac{1}{30}\right]$$

$$= \frac{1}{12}$$

Both the pipes can fill the tank in 12 minutes.

8. Option C

Net part filled in 1 hour = $\begin{bmatrix} \frac{1}{5} + \frac{1}{6} - \frac{1}{12} \end{bmatrix}$

$$= \frac{17}{60}$$
Therefore, the tank will be full in $\frac{60}{17}$ hrs. = $3 \times \frac{9}{17}$ hrs.

Capacity of t he tank
$$= (12 \times 13.5)$$
 litres $= 162$ litres

Number of buckets needed =
$$\left[\frac{162}{9}\right]$$
 = 18

10. Option B

Work done by the third pipe in 1 min.
$$= \frac{1}{50} - \left[\frac{1}{60} + \frac{1}{75} \right]$$
$$= \left[\frac{1}{50} - \frac{3}{100} \right]$$
$$= \frac{1}{100}$$

Therefore, the third pipe alone can empty the cistern in 100 min.

11. Option D

Net part filled in 1 hour
$$= \left[\frac{1}{4} - \frac{1}{9} \right]$$

 $= \frac{5}{36} \frac{1}{36}$ Therefore, the cistern will be filled in $\frac{3}{5}$ hours i.e. 7.2 hours

12. Option D

Part filled by (A + B) in 1 minute
$$= \left[\frac{1}{60} + \frac{1}{40}\right]$$

Suppose the tank is filled in x minutes = $\frac{\frac{1}{4}}{\frac{1}{24}}$

Then,
$$\frac{x}{2} \times \frac{1}{15} = 30 \text{ min.}$$

13. Option C

Let the slower pipe alone fill the tank in x minutes. Then, faster pipes will fill it in $\frac{x}{3}$ minutes

Therefore,
$$\frac{1}{x} + \frac{3}{x} = \frac{1}{36}$$

$$\frac{4}{x} = \frac{1}{36}$$

x = 144 min.

14. Option B

Time taken by one tap to fill the half tank = 3 hours

Part filled by the four taps in 1 hour
$$= \left[4 \times \frac{1}{6}\right]$$
$$= \frac{2}{3}$$

Remaining part =
$$\left[1 - \frac{1}{2}\right]$$

So, total time taken = 3 hours 45 minute

15. Option B

A's work in 1 hour =
$$\frac{1}{\frac{16}{4}}$$

B's work in 1 hour = $\frac{1}{\frac{16}{4}}$

$$(A + B)$$
's 2 hours work when opened alternately
$$= \left[\frac{1}{6} + \frac{1}{4}\right]$$

(A + B)'s 4 hours work when opened alternately
$$= \frac{5}{12}$$

$$= \frac{5}{6}$$

Remaining part =
$$\left[1 - \frac{5}{6}\right]$$

Therefore, total time to fill the tank (4 + 1) hours = 5 hours

Option E 16.

Let B be turned off after x minutes. Then, Part filled by (A + B) in x min + Part filled by A in (30 - x) min. = 1 So, x $\left[\frac{2}{75} + \frac{1}{45} \right] + (30 - x) \times \frac{2}{75} = 1$

17. Option E

Suppose pipe A alone takes x hours to fill the tank. Then, pipes B and C will take $\frac{x}{2}$ and $\frac{x}{4}$ hours respectively to fillthe tank.

So,
$$\frac{1}{x} + \frac{2}{x} + \frac{4}{x} = \frac{1}{5}$$

$$\frac{7}{x} = \frac{1}{5}$$

x = 35 hours

Option C 18.

(A + B)'s 1 hour work =
$$\begin{bmatrix} \frac{1}{12} + \frac{1}{12} \end{bmatrix} = \frac{9}{60} = \frac{3}{20}$$

(A + C)'s 1 hour work = $\begin{bmatrix} \frac{1}{12} + \frac{1}{12} \end{bmatrix} = \frac{8}{60} = \frac{2}{20}$
Part filled in 2 hours = $\begin{bmatrix} \frac{3}{20} + \frac{2}{15} \end{bmatrix} = \frac{17}{60}$
Part filled in 6 hours = $\begin{bmatrix} 3 \times \frac{17}{15} \end{bmatrix} = \frac{17}{20}$
Remaining part = $\begin{bmatrix} 1 - \frac{17}{20} \end{bmatrix} = \frac{3}{20}$

Now, it is the turn of A and B and $\frac{3}{20}$ part is filled by A and B in 1 hour.

So, total time taken to fill the tank = (6 + 1) = 7 hours

19. Option D

Part filled in 4 minutes =
$$4 \begin{bmatrix} 1 \\ 15 \end{bmatrix} = \frac{7}{15}$$

Remaining part = $\begin{bmatrix} 1 - \frac{7}{15} \end{bmatrix} = \frac{8}{15}$

Part filled by B in 1 minute = $\frac{1}{20}$

So, $\frac{1}{20} : \frac{8}{15} : 1 : x$
 $x = \begin{bmatrix} \frac{8}{15} \times 1 \times 20 \end{bmatrix} = 10 \frac{2}{3}$ minute = 10 minute 40 seconds

So, the tank will be full in (4 minute + 10 minute + 40 seconds) = 14 minute 40 seconds

20. Option C

Part filled in 2 hours =
$$\frac{2}{6} = \frac{1}{3}$$

Remaining part = $\left[1 - \frac{1}{3}\right] = \frac{2}{3}$
So, (A + B)'s 7 hours work = $\frac{2}{3}$
(A + B)'s 1 hour work = $\frac{2}{21}$

So, C's 1 hour work =
$$\left[(A + B + C)'s \text{ 1 hour work } \right] - (A + B)'s \text{ 1 hour's work} =$$

$$\left[\frac{1}{6} - \frac{2}{21} \right] = \frac{1}{14}$$

So, C alone can fill the tank in 14 hours.

21. Option D

Capacity of the tank $= (12 \times 13.5)$ litre = 162 litres

= $\frac{9 \text{ litres}}{162}$ = $\frac{162}{9}$ = 18 Capacity of each bucket Number of buckets needed

Option D 22.

Option D Part filled by (A + B + C) in 1 hour = $\left[\frac{1}{5} + \frac{1}{10} + \frac{1}{30}\right] = \frac{1}{3}$ So, all the three pipes together will fill the tank in 3 hours.

23. Option D

Half tank will be filled in 3 hours

Lets calculate remaining half,

Part filled by the four taps in 1 houir = $1 \times \frac{1}{6} = \frac{2}{3}$ Remaining part after $\frac{1}{2}$ filled = $1 - \frac{1}{2} = \frac{1}{2}$

$$\frac{2}{3}:\frac{1}{2}::1:x$$

$$x = \left[\frac{1}{2} \times 1 \times 32\right]$$

$$x = \left[\frac{1}{2} \times 1 \times 32\right]$$

$$x = \frac{3}{4} \text{ hours} = 45 \text{ mins.}$$

Total time = 3

hours +45 mins.

= 3 hours 45

mins

