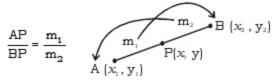
$$x = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, y = \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}$$



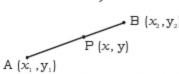
 The co-ordinate of the point P(x, y), dividing the line segment joining the two points A(x₁, y₁) and B (x₂, y₂) externally in the ratio m₁:m₂ are given by

$$x = \frac{m_1 x_2 - m_2 x_1}{m_1 - m_2}$$
, $y = \frac{m_1 y_2 - m_2 y_1}{m_1 - m_2}$

$$\frac{\text{AP}}{\text{BP}} = \frac{\mathbf{m_1}}{\mathbf{m_2}} \qquad \text{A} \left(x_1, y_1\right)$$

 The co-ordinates of the mid-point of the line segment joining the two points A(x₁, y₁) and B (x₁, y₁) are given by

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$



Division by Axes: If $P(x_1, x_2)$ and $Q(x_2, y_2)$, then PQ is divided by

(i)
$$x$$
 - axis in the ratio = $\frac{-y_1}{y_2}$

(ii) y - axis in the ratio =
$$-\frac{x_1}{x_2}$$

Division by a Line: A line ax + by + c = 0

divides PQ in the ratio =
$$-\frac{ax_1 + by_1 + c}{ax_2 + by_2 + c}$$

 Area of a triangle: The area of a triangle ABC whose vertices are (x₁, y₁), B(x₂, y₂) and C(x₃, y₃) is denoted by Δ.

$$\triangle = \frac{1}{2} \begin{bmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{bmatrix}$$

$$= \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

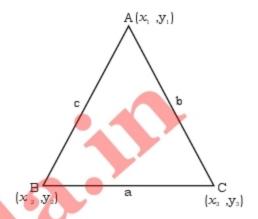
♦ Area of Polygon: The area of the polygon whose vertices are (x₁, y₁), (x₂, y₂),.....(x_k, y_k) is -

$$\Delta = \frac{1}{2} \begin{bmatrix} (x_1 \mathbf{y_2} - x_2 \mathbf{y_1}) + (x_2 \mathbf{y_3} - x_3 \mathbf{y_2}) + \dots \\ (x_n \mathbf{y_1} - x_1 \mathbf{y_n}) \end{bmatrix}$$

- ♦ Some Important Points in a Triangle :
- Centroid: If (x₁, y₁), (x₂, y₂) and (x₃, y₃) are the vertices of a triangle, then the co-ordinates of its centroid are -

$$\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$$

Incentre: If A (x₁, y₁), B(x₂, y₂) and C(x₃, y₃) are the vertices of a Δ ABC s.t. BC = a, CA = b and AB = c, then the co-ordinates of its incentre are



$$\left(\frac{ax_1 + bx_2 + cx_3}{a + b + c}, \frac{ay_1 + by_2 + cy_3}{a + b + c}\right)$$

Circumcentre: If A(x₁, y₁), B(x₂, y₂) and C(x₃, y₃) are the vertices of a Δ ABC, then the coordinates of its circumcentre are

$$\left(\frac{x_1 \sin 2A + x_2 \sin 2B + x_3 \sin 2C}{\sin 2A + \sin 2B + \sin 2C}\right),$$

$$\frac{y_1 \sin 2A + y_2 \sin 2B + y_3 \sin 2C}{\sin 2A + \sin 2B + \sin 2C}$$

· Orthocentre: Co-ordinates of orthocentre are

$$\left(\frac{x_1 \tan A + x_2 \tan B + x_3 \tan C}{\tan A + \tan B + \tan C}\right)$$

$$\frac{y_1 \tan A + y_2 \tan B + y_3 \tan C}{\tan A + \tan B + \tan C}$$

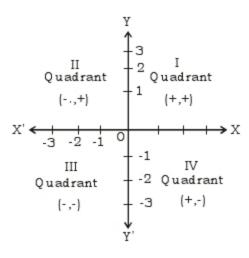
Note

- If the traingle is equilateral, then centroid, incentre, orthocentre, circumcentre coincides.
- Orthocentre, centroid and circumcentre are always collinear and centroid divides the line joining orthocentre and circumcentre in the ratio 2:1.
- In an isosceles triangle centroid, orthocentre, incentre, circumcentre lies on the same line.
- Incentre divides the angles bisectors in the ratio (b + c): a, (c + a): b, (a + b): c.

CO-ORDINATE GEOMETRY

♦ CARTESIAN CO-ORDINATE SYSTEM:

Rectangular Co-ordinate System: Let X'OX and Y'OY be two mutually perpendicular lines through any point O in the plane of the paper. Point O is known as the origin. The line X'OX is called the x-axis or axis of x; the line Y'OY is known as the y-axis or axis of y, and the two lines taken together are called the co-ordinates axes or the axes of co-ordinates.



Region	Quad- rant	Nature of X and Y	Signs of co-ordin- ate
XOY	I	x > 0, y > 0	(+, +)
AOX,	П	x < 0, y > 0	(-,+)
X,OA,	III	x < 0, y < 0	(-, -)
Y'OX	IV	x > 0, y < 0	(+, -)

Note - Any point lying on x-axis or y-axis does not lie in any quadrant.

Any point can be represented on the plane described by the co-ordinate axes by specifying its x and y co-ordinates.

The x-co-ordinate of the point is also known as the abscissa while the y-coordinate is also known as the ordinate.

◆ Distance Formula : The distance two point A(x₁, y₁) and B(x₂, y₂) is given by

AB =
$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



Note:

- Distance is always positive. Therefore, we often write AB instead of |AB|.
- 2. The distance of a point P (x, y) from the ori-

$$gin = \sqrt{x^2 + y^2}$$

3. The distance between two polar co-ordinates

A
$$(r_1, \theta_1)$$
 and B (r_2, θ_2) is given by
AB = $\sqrt{r_1^2 + r_2^2 - 2r_1r_2\cos(\theta_1 - \theta_2)}$

♦ Application of Distance Formulae :

- (i) For given three points A, B, C to decide whether they are collinear or vertices of a particular triangle. After finding AB, BC and CA we shall find that the points are:
- Collinear (a) If the sum of any two distances is equal to the third

- (b) If are of ∆ ABC is zero
- (c) If slope of AB = slope of BC = slope of CA.
- Vertices of an equilateral triangle if AB = BC = CA
- Vertices of an isosceles triangle if AB = BC or BC = CA or CA = AB.
- Vertices of a right angled triangle if AB² + BC² = CA² etc.

(ii) For given four points A,B,C,D:

- AB = BC = CD = DA and AC = BD ⇒ ABCD is a square.
- AB = BC = CD = DA and AC ≠ BD ⇒ ABCD is a rhombus.
- AB = CD, BC = DA and AC = BD ⇒ ABCD is a recatangle.
- AB = CD, BC = DA and AC ≠ BD ⇒ ABCD is a parallelogram.

Note:

- The four given points are collinear, if Area of qaudrilateral ABCD is zero.
- Diagonals of square, rhombus, rectangle and parallelogram always bisect each-other.
- Diagonals of rhombus and square bisect each other at right angle.

• Section Formuale :

1. The co-ordinates of a point P(x, y), dividing the line segment joining the two points $A(x_1,y_1)$ and $B(x_2,y_2)$ internally in the ratio $m_1:m_2$ are given by

 Area of the triangle formed by co-ordinate axes and the line a x + b y + c = 0

is
$$\frac{c^2}{2ab}$$

 Straight Line: A straight line is a curve such that every point on the line segment joining any two points on it lies on it.

Different Forms of the Equations of a Straight Line :

(a) General Form: The general Form of the equation of a straight line is ax + by + c = 0 (First degree equation in x and y). Where a, b and c are real constants and a, b are not simultaneously equal to zero.

In this equation, slope of the line is given

by
$$-\frac{a}{b}$$
.

The general form is also given by y = mx + c; where m is the slope and c is the intercept on y-axis.

(b) Line Parallel to the X-axis: The equation of a straight line to the x-axis and at a distance b from it, is given by y = b

Obviously, the equation of the x-axis is y = 0

(c) Line Parallel to Y-axis: The equation of a straight line parallel to the y-axis and at a distance a from is given by x = a obviously, the equation of y-axis is x = 0

(d) Slope Intercept Form: The equation of a striaght line passing through the point A[x₁, y₁] and having a slope m is given by

$$(y - y_1) = m(x - x_1)$$

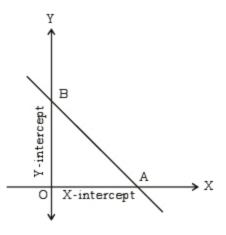
(e) Two Points Form: The equation of a straight line passing through two points A(x, y,) and B(x, y,) is given by

$$(y - y_1) = \left(\frac{y_2 - y_1}{x_2 - x_1}\right)(x - x_1)$$

Its slope (m) =
$$\frac{y_2 - y_1}{x_2 - x_1}$$

(e) Intercept Form: The equation of a straight line making intercepts a and b on the axes of x and y respectively is given by

$$\frac{x}{a} + \frac{y}{b} = 1$$



Slope (Gradient) of a Line :

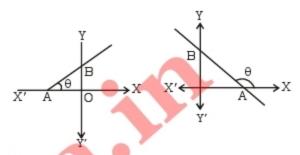
$$m = \tan \theta = -\frac{a}{b}$$

$$\{ \therefore ax + by + c = 0 \Rightarrow y = -\frac{a}{b}x - \frac{c}{b} \}$$

$$\Rightarrow$$
 y = mx + c, where m = $-\frac{a}{b}$ and c is a con-

stant }

Here m is called the slope or gradient of a line and c is the intercept on y-axis. The slope of a line is always measured in anticlockwise.



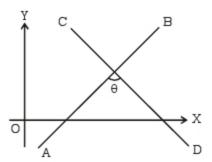
Slope of a line in terms of co-ordinates any two points on it:-

If (x_1, y_1) and (x_2, y_2) are co-ordinates of any two points on a line, then its slope is

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\text{Difference of ordinates}}{\text{Difference of abscissa}}$$

Angle between two lines :

$$\tan\theta = \pm \left(\frac{m_2 - m_1}{1 + m_1 m_2}\right)$$



 Condition of Parallellism of lines: If the slopes of two lines is m₁ and m₂ and if they are parallel, then,

 Length of Perpendicular it y or Distance of a Point from a Line: The length of perpendicular from a given point (x1, y1) to a line ax + by + c = 0 is:

$$\frac{\left| ax_1 + by_1 + c \right|}{\sqrt{a^2 + b^2}}$$

Note: The length of Perpendicular from the t

origin to the line ax + by + c = 0 is given by

$$\frac{|c|}{\sqrt{a^2 + b^2}}$$

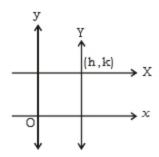
Distance between two Parallel Lines : If two lines are parallel, the distance between them will always be the same.

When two straight lines are parallel whose equations are $ax + by + c_1 = 0$ and $ax + by + c_1 = 0$, then the distance between

them is given by $\frac{\left|c_1-c_2\right|}{\sqrt{a^2+b^2}}$.

Changes of Axes: If origin (0,0) is shifted to (h, k) then the coordinates of the point (x, y)referred to the old axes and (X, Y) referred to the new axes can be related with the rela-

$$x = X + h$$
 and $y = Y + k$



- Point of Intersection of Two Lines: Point of intersection of two lines can be obtained by solving the equations as simultaneous equa-
- If the given equations of straight line are $a_1x + b_1y + c_1 = 0$ and $a_1x + b_2y + c_2 = 0$, then
- (i) The angle between the lines 'θ' is given by

$$\tan \theta = \frac{a_2 b_1 - a_1 b_2}{a_1 a_2 + b_1 b_2}$$

(ii) If the lines are parallel, then

$$a_3b_1 - a_1b_3 = 0$$
 or $\frac{a_1}{a_2} = \frac{b_1}{b_2}$

(iii) If the lines are perpendicular, then $a_1a_1 + b_1b_2 = 0$

(iv) Coincident: $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$

 Angle between lines $x \cos \alpha + y \sin \alpha = P_1$ and $x \cos \beta + y \sin \beta = P$, is $|\alpha - \beta|$

Exercise

----- LEVEL - 1 ------

- The point (-5, 7) lies in the quadrant :
 - (a) First
- (b) Second
- (c) Third
- (d) Fourth
- The point (7, -5) lies in the quadrant :
 - (a) First
- (b) Second
- (c) Third
- (d) Fourth
- 3. Find the distance between the points (-6,2) and (2, 4):
 - (a) 2√17
- (b) 4√17
- (c) $2\sqrt{5}$
- (d) 10
- 4. The distance between the points A(b,o) and B (0, a) is:
 - (a) $\sqrt{a^2 b^2}$ (b) $\sqrt{a^2 + b^2}$
 - (c) $\sqrt{a+b}$ (d) a+b
- The distance between the points A (7, 4) and B(3,1) is
 - (a) 6 units
- (b) 3 units
- (c) 4 units
- (d) 5 units
- The co-ordinates of point situated on x-axis at a distance of 5 units from y-axis is :
 - (a) (0, 5)
- (b) (5,0)
- (c) (5, 5)
- (d) (-5,5)
- The co-ordinates of a point situated on yaxis at a distance of 7 units from x-axis is
 - (a)(0,7)
- (b) (7,0)
- (c) (7, 7)
- (d) (-7,7)
- 8. The co-ordinates of a point below x-axis at a distance of 6 units from x-axis but lying on y-axis is :
 - (a)(0,6)
- (b)(-6,0)
- (c)(0,-6)
- (d)(6,-6)
- 9. The distance of the point (6, -8) from the origin is:
 - (a) 2 units
- (b) 14 units
- (c) 7 units
- (d) 10 units
- 10. The point of intersection of the lines 2x +7y = 1 and 4x + 5y = 11 is:
 - (a)(4,-1)
- (b)(2,3)
- (c) (-1, 4)
- (d)(4,-2)
- 11. The line 4x + 7y = 12 meets x -axis at the point:
 - (a) (3, 1)
- (b)(0,3)
- (c)(3,0)
- (d)(4,0)
- 12. The line 4x 9y = 11 meets y-axis at the point:
 - (a) $\left(-\frac{11}{9},0\right)$ (b) $\left(0,-\frac{11}{9}\right)$
 - (c) $\left(0, \frac{11}{4}\right)$ (d) $\left(0, -\frac{11}{4}\right)$
- 13. The slope of the line 3x + 7y + 8 = 0 is :

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(a) parallel

(c) coincident

(b) perpendicualr (d) intersecting

Fo	r More Boo	ok Download Ge
	(a) 3	(b) 7
	(c) $-\frac{3}{7}$	(d) $\frac{3}{7}$
14.	The slope of the Q(2,3) is:	line joining P(-4, 7) and
	(a) $-\frac{2}{3}$	(b) ² / ₃
	(c) $-\frac{3}{2}$	(d) $\frac{3}{2}$
15.		line parallel to x -axis at aits and above x -axis is: (b) $y = 6x$
16.	(c) x = 6y The equation of a	(d) $y = 6$ line parallel to y -axis at lits to the left of y -axis, is
17.	(c) $x + 5y = 0$ The equation of	(b) $x = -5$ (d) $y + 5x = 0$ a line parallel to x -axis of 7 units below x -axis
18.	(a) $y = -7$ (c) $x = -7$ The area of the tr	(b) x = 7 (d) y = -7x iangle whose vertices are and R (3, -4), (in square
	(a) 66	(b) $16\frac{1}{2}$
19.	the vertices of a t	(d) 35), B(0, 3) and C(4, 0) are triangle which is:
20.	(c) Equilateral The co-ordinates	(b) Right angled (d) None of these of the centroid of △PQR , O), Q(9, -3) and R(8,3)
	(a) (1,0)	(b) $\left(\frac{19}{3}\text{p}\right)$
21.	(c) (0,5) The equation of a points A (0, -3) an	(d) (5,0) line passing through the id B(-5,2) is:
22.	(a) $x+y+3=0$ (c) $x-y+3=0$ The length of per gin to the line 12: (a) 2 units	(d) $x-y-3=0$ pendicular from the ori-
	(c) $\frac{7}{13}$ units	(d) $\frac{7}{11}$ units
23.		he line joining the points $\sqrt{5}$ makes with x-axis is
	: (a) 30° (c) 60°	(b) 45° (d) 90°

24. The lines whose equations are 2x - 5y + 7= 0 and 8x - 20y + 28 = 0 are:

Ε,	LEVEL - 2
1.	If the distance of the point $P(x, y)$ from $A(a, 0)$ is $a + x$, then $y^a = ?$
2.	(a) $2 ax$ (b) $4ax$ (c) $6ax$ (d) $8ax$ If the point (x, y) is equidistant from the points $(a+b, b-a)$ and $(a-b, a+b)$ then $bx = ?$
3.	(a) a ² y (b) ay ² (c) ay (d) a ² y ² If the sum of the square of the distance of the point (x, y) from the point (a, 0) and (-a, 0) is 2b ² , then:
4.	(a) $x^3 + a^2 = b^2 + y^2$ (b) $x^3 + a^2 = 2b^2 - y^2$ (c) $x^3 - a^2 = b^2 + y^2$ (d) $x^3 + a^2 = b^2 - y^2$ P (-4, a) and Q(2, a + 4) are two points and the co-ordinates of the middle point of PQ are (-1, 4). The value of a is:
5.	(a) 0 (b) 2 (c) -2 (d) 3 If the points P(2, 3), Q(5, a) and R(6, 7) are collinear, the value of a is:
6	(a) 5/2 (b) - 4/3 (c) 6 (d) 5
0.	The equation of a line parallel to x-axis and passing through (-6,-5) is:
	(a) $y = -5$ (b) $x = -6$
7.	(c) $y = -5x$ (d) $y = -6x - 5$ The equation of a line parallel to y-axis and passing through $(2, -5)$ is:
8.	(a) $x = 2$ (b) $y = -5$ (c) $y = 2x$ (d) $x = -5y$ Two vertices of a triangle PQR are P(-1, 0) and Q(5, -2) and its centroid is (4, 0). The co-ordinates of R are:
9.	(a) $(8,-2)$ (b) $(8,2)$ (c) $(-8,2)$ (d) $(-8,-2)$ The co-ordinates of the point of intersection of the medians of a triangle with vertices $P(0,6)$, $Q(5,3)$ and $R(7,3)$ are :
10.	(a) (4,5) (b) (3,4) (c) (4,4) (d) (5,4) The ratio in which the line segment joining A(3,-5) and B(5,4) is divided by x-axis is:
11.	(a) $4:5$ (b) $5:4$ (c) $5:7$ (d) $6:5$ The ratio in which the line segment joining $P(-3,7)$ and $Q(7,5)$ is divided by y-axis is:
	(a) 3:7 (b) 4:7 (c) 3:5 (d) 4:5
12.	The ratio in which the point $P\left(1, \frac{10}{3}\right)$ divides the join of the point A(-3, 2) and B(3,
	vizes the join of the point A(-5, 2) and B(5,

- 4) is :
- (a) 2:3
- (b) 1:2
- (c) 2 : 1
- (d) 3:1
- The equation of a line with slope 5 and passing through the point (-4, 1) is :
 - (a) y = 5x + 21
- (b) y = 5x 21
- (c) 5y = x + 21
- (d) 5y = x 21
- 14. The value of a so that the lines x + 3y 8 =0 and ax + 12y + 5 = 0 are parallel is :
 - (a) 0
- (b) 1
- (c) 4
- (d) 4
- 15. The value of P for which the lines 3x + 8y +9 = 0 and 24x + py + 19 = 0 are perpendicualar is :
 - (a) 12
- (b) -9
- (c) 11
- (d)9
- The value of a so that line joining P(-2, 5) and Q (0, -7) and the line joining A (-4, -2) and B(8, a) are perpendicular to each other
 - (a) -1
- (b)5
- (c) 1
- (d) 0
- 17. The angle between the lines represented by the equations $2y - \sqrt{12}x - 9 = 0$ and $\sqrt{3}y$ -x + 7 = 0, is:
 - (a) 30°
- (b) 45°
- (c) 60°
- (d) $22\frac{1^{\circ}}{2}$
- If P(3, 5), Q (4, 5) and R(4, 6) be any three points, the angle between PQ and PR is (a) 30° (b) 45°
- (c) 60°
- (d) 90°
- Given a ΔPQR with vertices P (2, 3), Q (-3, 7) and R (-1, -3). The equation of median
 - (a) x-y+10=0 (b) x-4y-10=0
 - (c) x 4y + 10 = 0 (d) None of these
- 20. The co-ordinates of the point P which di-

vides the join of A(3, -2) and B $\left(\frac{11}{2}, \frac{21}{2}\right)$ in

the ratio 2:3 are:

- (a) (4, 3)
- (c) $\left(4, \frac{5}{2}\right)$ (d) $\left(\frac{3}{2}, \frac{7}{2}\right)$

----- LEVEL - 3 --

- The length of the portion of the straight line 8x + 15y = 120 intercepted between the axes is:
 - (a) 14 units
- (b) 15 units
- (c) 16 units
- (d) 17 units
- 2. The equation of the line passing through the point (1, 1) and perpendicular to the line 3x + 4y - 5 = 0, is:
 - (a) 3x + 4y 7 = 0 (b) 3x + 4y + k = 0
 - (c) 3x 4y 1 = 0 (d) 4x 3y + 1 = 0

- The equation of a line passing through the point (5, 3) and parallel to the line 2x - 5y +3 = 0, is:
 - (a) 2x 5y 7 = 0 (b) 2x 5y + 5 = 0
 - (c) 2x 2y + 5 = 0 (d) 2x 5y = 0
- The sides PQ, QR, RS and SP of a quadrilateral have the equations x + 2y = 3, x = 1, x-3y=4, 5x+y+12=0 respectively, then the angle between the diagonals PR and QS
 - (a) 30°
- (b) 45°
- (c) 60°
- (d) 90°
- The equations of two equal sides of an isosceles triangle are 7x - y + 3 = 0 and x + y -3 = 0 and its third side passes through the point (1,-10). The equation of the third side
 - (a) x 3y 31 = 0 but not x 3y 31 = 0
 - (b) neither 3x + y + 7 = 0 nor x 3y 31 = 0
 - (c) 3x + y + 7 = 0 or x 3y 31 = 0
 - (d) 3x + y + 7 = 0 but not x 3y 31 = 0
- If P, and P, be perpendicular from the origin upon the straight lines $x \sec \theta + y$ cosecθ = a and x cosθ – y sin θ = a cos 2θ

respectively, then the value of $4P_1^2 + P_2^2$ is

- (a) a²
- (b) 2a2
- (c) $\sqrt{2} a^2$
- (d) 3a²
- 7. Find the equation of the line passing through the point (2, 2) and cutting off intercepts on the axes whose sum is 9?
 - (a) x + 2y 6 = 0 but not 2x + y 6 = 0
 - (b) neither x + 2y 6 = 0 nor 2x + y 6 = 0
 - (c) 2x + y 6 = 0 but not x + 2y 6 = 0
 - (d) x + 2y 6 = 0 or 2x + y 6 = 0

ANSWER KEY

LEVEL - 1

5. (d)

1.(b) 2. (d)

6.(b)

- 3. (a)
 - 4. (b) 7. (a) 8. (c)
- 10. (a) 9. (d) 13. (c) 14. (a)
- 11.(c)
- 12.(b) 15. (d) 16.(b)
- 18. (c) 17. (a) 21. (a) 22. (c)
- 19.(b) 23. (a)
- 20. (d) 24. (c)

LEVEL - 2

2.(c) 1.(b) 5. (c) 6. (a)

10.(b)

- (d) 7. (a)
- 11. (a)
- 8. (b) 12. (c)

4. (b)

- 13. (a) 14. (c) 17. (a) 18. (b)
- 15. (b) 19. (c)
- 16. (d) 20. (a)

LEVEL - 3

9. (c)

- 1.(d) 2.(c) 5. (c) 6. (a)
- 3.(b) 7.(d)
- 4. (d)

Hints and Solutions :

LEVEL - 1

LEVEL - I

The point (-5, 7) lies in the second quadrant.

 (d) The point (7, -5) lies in the fourth quad-

(a) Distance between two points

$$=\sqrt{(x_2-x_1)^2+(y_2-y_1)^2}$$

here $(x_1, y_1) = (-6, 2)$ and $(x_2, y_2) = (2, 4)$ \therefore Required distance =

$$=\sqrt{(-6-2)^2+(2-4)^2}$$

$$=\sqrt{64+4}=\sqrt{68}=2\sqrt{17}$$
 unit

4. (b)

$$AB = \sqrt{(b - 0)^{2} + (0 - a)^{2}} = \sqrt{b^{2} + a^{2}}$$
$$= \sqrt{a^{2} + b^{2}}$$

5. (d) $AB^2 = (7-3)^2 + (4-1)^2 = 4^2 + 3^2 = 16 + 9 = 25$ $\Rightarrow AB = \sqrt{25} = 5 \text{ units}$

 (b) Clearly, the point of x -axis has ordinate 0 and abscissa 5.

(a)
 Clearly, the point on y-axis has abscissa 0.
 So, the point is (0, 7)

8. (c) Clearly, the point is (0, 6)

So, the point is (5,0)

9. (d)

Required distance =
$$\sqrt{(6-0)^2 + (-8-0)^2}$$

$$=\sqrt{36+64}=\sqrt{100}=10$$
 units

10. (a)

$$2x + 7y = 1$$
(i)

$$4x + 5y = 11 \dots (ii)$$

on solving (i) and (ii), we get x = 4 and y = -1

∴ Required point of intersection = (4, -1)

11.(c)
 Equation of x-axis is y = 0
 put y = 0 in 4x + 7y = 12 we get x = 3
 ∴ Required point = (3,0)

12. (b)

Equation of y-axis is x = 0

put
$$x = 0$$
 in $4x - 9y = 11$ we get $y = -\frac{11}{9}$

 $\therefore \text{ Required point } = \left(0, -\frac{11}{9}\right)$

13. (c)
$$3x + 7y + 8 = 0 \Rightarrow 7y = -3x - 8$$

$$\Rightarrow y = \left(-\frac{3}{7}\right)x - \left(\frac{8}{7}\right)$$

:. Slope of the line is = $-\frac{3}{7}$

14. (a)

Slope of PQ =
$$\frac{y_2 - y_1}{x_2 - x_1} = \frac{3 - 7}{2 - (-4)} = \frac{-4}{6} = -\frac{2}{3}$$

15. (d)

Clearly; the equation of the line is, y = 6

16. (b)

Clearly, the equation of the line is, x = -5

17. (a)

Clearly, the equation of the line is y = -7

18. (c)

$$\Delta = \frac{1}{2} \left[x_1 \left(y_2 - y_3 + x_2 y_3 - y_1 + \right) x_3 y_1 - y_2 \right]$$

$$= \frac{1}{2} |4(4+8) - 3(-4-5) + 3(5-8)|$$

$$=\frac{1}{2}|66|=33 \text{ sq. units}$$

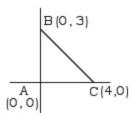
19. (b)

$$AB = \sqrt{(0+0)^2 + (0-3)^2} = 3$$

$$AC = \sqrt{(4-0)^2 + (0+0)^2} = 4$$

and BC =
$$\sqrt{(4-0)^2 + (0-3)^2} = 5$$

∴ ΔABC is a right angled triangle.



20. (d)

The co-ordinates of the centroid of $\triangle PQR$ are -

$$\left(\frac{-2+9+8}{3}, \frac{0-3+3}{3}\right) = (5,0)$$

21. (a)

The required equation is

$$(y+3) = \frac{2+3}{-5-0}(x-0)$$

$$\Rightarrow$$
y+3=-x \Rightarrow x+y+3=0

22. (c)

Length of perpendicular =

$$= \frac{12 \times 0 + 5 \times 0 + 7}{\sqrt{12^2 + 5^2}} - \frac{7}{13} \text{ units}$$

23. (a)

The slope of the line is $\frac{\sqrt{5}-1}{\sqrt{15}-\sqrt{3}} = \frac{1}{\sqrt{3}}$

 $\therefore \tan \theta = \frac{1}{\sqrt{3}} \text{ or } \theta = 30^{\circ}$

24. (c)

$$\frac{a_1}{a_2} = \frac{2}{8} = \frac{1}{4}$$
, $\frac{b_1}{b_2} = \frac{-5}{-20} = \frac{1}{4}$ and $\frac{c_1}{c_2} = \frac{7}{28} = \frac{1}{4}$

 $\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$, So the given lines are coincident.

LEVEL - 2

1. (b)

$$\sqrt{(x-a)^2 + (y-0)^2} = a + x$$

$$\Rightarrow (x-a)^2 + y^2 = (a+x)^2$$

$$\Rightarrow y^2 = (x+a)^2 - (x-a)^2$$

$$\Rightarrow y^2 = 4ax$$

2. (c)

Let (x, y), Q(a + b, b - a) and R(a - b, a + b) are given points.

$$\Rightarrow \sqrt{(x-(a+b))^2+(y-(b-a))^2}$$

$$= \sqrt{(x - (a - b))^2 + (y - (a + b))^2}$$

 $\Rightarrow x^2 - 2x(a+b) + (a+b)^2 + y^2 - 2y(b-a) + (b+a)^2 = x^2 + (a-b)^2 - 2x(a-b) + y^2 + (a+b)^2$

$$\Rightarrow$$
 ax + bx + by - ay = ax - bx + ay + by

$$\Rightarrow$$
 2b x = 2ay

$$\Rightarrow$$
 bx = ay.

(d)

Let A (x, y), P(a, 0) and Q(-a, 0), Then,

$$\Rightarrow AP^2 + AQ^2 = 2b^2$$

$$\Rightarrow [(x-a)^2 + (y-0)^2] + [(x+a)^2 + (y-0)^2] = 2b^2$$

$$\Rightarrow x^2 + a^2 - 2ax + y^2 + x^2 + a^2 + 2ax + y^2 = 2b^2$$

$$\Rightarrow 2(x^2 + a^2 + y^2) = 2b^2$$

$$\Rightarrow x^2 + a^2 + y^2 = b^2$$

$$\Rightarrow x^2 + a^2 = b^2 - y^2$$

4. (d)

co-ordinates of middle point = (-1, 4)

$$\frac{a+a+4}{2} = 4 \Rightarrow 2a+4=8 \Rightarrow 2a=4$$

5. (c

Since, P,Q and R collinear

$$\Rightarrow \frac{a-3}{5-2} = \frac{7-3}{6-2} \Rightarrow \frac{a-3}{3} = \frac{4}{4}$$

6. (a)

The equation of a line parallel to x-axis is y = b.

Since, it passes through (-6, -5), so b = -5The required equation is, y = -5

7. (a)

The equation of a line parallel to y-axis is, x = a.

Since, it passes through (2, -5), so a = 2

... The required equation is, x = 2

8. (b)

Let the co-ordinates of R be (x, y). Then,

$$\frac{-1+5+x}{3}$$
 = 4 and $\frac{0-2+y}{3}$ = 0

or
$$4 + x = 12$$
 and $-2 + y = 0$

$$R = (x, y) = (8, 2)$$

9. (c)

Since, point of intersection of median is "centroid".

. co-ordinates of centroid

$$= \left(\frac{0+5+7}{3}, \frac{6+3+3}{3}\right)$$

$$=\left(\frac{12}{3},\frac{12}{3}\right)$$

10. (b)

Let the ratio be k: 1

The ordinate of a point lying on x-axis must

$$\frac{4k-5\times1}{k+1}=0 \Rightarrow 4k=5 \Rightarrow k=\frac{5}{4}$$

$$\therefore$$
 Required ratio is $\frac{5}{4}:1=5:4$

11. (a)

Let the ratio be k: 1

The abcissa of a point lying on y-axis must be zero

$$\frac{7k-3\times1}{k+1} = 0 \Rightarrow 7k-3 = 0 \Rightarrow k = \frac{3}{7}$$

 \therefore Required ratio is $\frac{3}{7}:1=3:7$

12.(c)

Let the ratio be k:1

$$\frac{3k-3\times1}{k+1}=1$$

$$\Rightarrow$$
 3k-3 = k+1 \Rightarrow 2k = 4 \Rightarrow k = 2

. Required ratio is 2:1

13. (a)

Let the equation be y = 5x + c

Since it passes through (-4, 1), we have 1 = 5(-4) + c

c = 21 so, its equation is, y = 5x + 21

14. (c)

Condition of parallelism $\frac{a_1}{a_2} = \frac{b_1}{b_2}$

$$\therefore \frac{1}{a} = \frac{3}{12} \Rightarrow a = 4$$

Alternatively,

$$x + 3y - 8 + 0 \Rightarrow y = \left(-\frac{1}{3}\right)x + \left(\frac{8}{3}\right)x \cdot m_1 = -\frac{1}{3}$$

$$ax+12y+5+0=0 \Rightarrow y=\left(-\frac{a}{12}\right)x-\frac{5}{12}$$

$$m_2 = -\frac{a}{12}$$

for parallelism, m₁ = m₂

$$\frac{1}{12} = -\frac{a}{12} \Rightarrow a = 4$$

15. (b)

Condition of perpendicularism, a₁a₂ + b₁b₂

Alternatively-

 $3x + 8y + 9 = 0 \Rightarrow$

$$y = \left(-\frac{3}{8}\right)x - \frac{9}{8}$$
 : $m_1 = -\frac{3}{8}$

$$24x + py + 19 = 0 \Rightarrow y = \left(-\frac{24}{p}\right)x - \frac{19}{p}$$

$$m_2 = -\frac{24}{p}$$

for perpendicularism, $m_1 \cdot m_2 = -1$

$$\therefore = \left(-\frac{3}{8}\right) \left(-\frac{24}{p}\right) = -1$$

16. (d)

$$m_1 = \text{Slope of PQ} = \frac{-7 - 5}{0 + 2} = \frac{-12}{2} = -6$$

$$m_3 = \text{Slope of AB} = \frac{a+2}{8+4} = \frac{a+2}{12}$$

$$m_1 m_2 = -1 \implies -6 \times \frac{a+2}{12} = -1$$

17. (a)

$$2y - \sqrt{12}x - 9 = 0 \Rightarrow y = \frac{\sqrt{12}}{2}x + \frac{9}{2}$$

$$\Rightarrow$$
 m₁ = $\frac{\sqrt{12}}{2}$ = $\sqrt{3}$

$$\sqrt{3}y - x + 7 = 0 \Rightarrow y = \left(\frac{1}{\sqrt{3}}\right)x - \frac{7}{\sqrt{3}}$$

$$\Rightarrow$$
 m₂ = $\frac{1}{\sqrt{3}}$

$$\therefore \tan \theta = \frac{m_1 - m_2}{1 + m_1 \cdot m_2} = \frac{\sqrt{3} - \frac{1}{\sqrt{3}}}{1 + \sqrt{3} \cdot \frac{1}{\sqrt{3}}} = \frac{1}{\sqrt{3}}$$

18. (b)

Slope of PQ,
$$m_1 = \frac{5-5}{4-3} = 0$$

Slope of PR,
$$m_2 = \frac{6-5}{4-3} = 1$$

$$\therefore \tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right| = \left| \frac{0 - 1}{1 + 0} \right| = 1$$

So,
$$\theta = 45^{\circ}$$

19. (c)

Clearly, M is the mid-point of QR.

Co-ordinates of M are
$$\left(\frac{-3-1}{2}, \frac{7-3}{2}\right)$$

i.e. (-2, 2)

Now, find the equation of the line joining P(2,3) and M(-2,2)

Required equation is , $(y-3) = \frac{2-3}{-2-2}(x-2)$

$$\Rightarrow y - 3 = \frac{1}{4}(x - 2) \Rightarrow 4y - 12 = x - 2$$

$$\Rightarrow x - 4y + 10 = 0$$

20. (a)

Required point is :

$$\left(\frac{3\times3+2\times\frac{11}{2}}{3+2},\,\frac{3(-2)+2\frac{21}{2}}{3+2}\right)$$

$$=\left(\frac{20}{5},\frac{15}{5}\right)=(4,3)$$

LEVEL - 3

1. (d)

Point of intersection at x -axis = (x, 0)

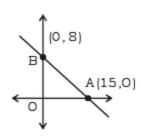
$$x = 8x + 15 y = 120$$

$$\Rightarrow$$
 8x + 15 × 0 = 120 \Rightarrow x = 15

Point of intersection at y-axis = (0, y)

$$x = 8x + 15y = 120$$

$$\Rightarrow$$
 0 + 15y = 120 \Rightarrow y = 8



$$= \sqrt{(15-0)^2 + (0-8)^2}$$
$$= \sqrt{225+64} = \sqrt{289}$$
$$= 17 \text{ units}$$

2. (c)

Given line -
$$3x + 4y - 5 = 0 \Rightarrow y = \left(-\frac{3}{4}\right)x + \frac{5}{4}$$

 $\therefore \text{ its slope, } m_1 = -\frac{3}{4}$

Let m, be the slope of required line.

Then,
$$m_1 m_2 = -1$$
 or $\left(-\frac{3}{4}\right)$ m2 = -1

$$\Rightarrow m_3 = \frac{4}{3}$$

Let the required equation be, $y = m_x x + c$

$$\Rightarrow$$
 y = $\frac{4}{3}x + c$

Since, it passes through (1, 1)

$$1 = \frac{4}{3} \times 1 + c \Rightarrow c = 1 - \frac{4}{3} = -\frac{1}{3}$$

: the required equation is , $y = \frac{4}{3}x - \frac{1}{3}$

or
$$4x - 3y - 1 = 0$$

3. (b)

$$2x - 5y + 3 = 0$$

$$\Rightarrow$$
 y = $\left(\frac{2}{5}\right)x + \left(\frac{3}{5}\right)$

 $\therefore its slope m_1 = \frac{2}{5}$

Let the slope of line which is parall;el to the given line is m_a

$$m_2 = m_1 = \frac{2}{5}$$

Let the required equation be, $y = \frac{2}{5}x + c$

Since, it passes through (5, 3)

$$3 = \frac{2}{5} \times 5 + c \Rightarrow c = 1$$

 $\therefore \text{ Required equation is, } y = \frac{2}{5}x + 1$

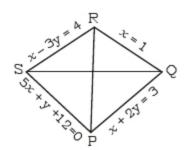
or
$$2x - 5y + 5 = 0$$

4. (d)

$$x + 2y = 3$$
(i)

$$5x + y = -12$$
(ii)

On solving (i) and (ii), we get x = -3, y = 3 \therefore co-ordinates of P(-3,3)



Similarly, Q(1,1), R(1,-1) and S(-2,2)

Now, $m_1 = \text{slope of PR} = \frac{-1 - 3}{1 + 3} = -1$

$$m_a = slope of QS = \frac{-2-1}{-2-1} = 1$$

∴ m₁m₂ = -1

... the required angle is 90°

5. (c)

... Third side passes through (1, -10) so its equation y + 10 = m(x - 1)(i)

This side makes equal angle with the given two sides.

let this angle be θ.

Now, slope of line 7x - y + 3 = 0 is m_1 ,

and slope of line x + y - 3 = 0 is m_a ,

angle between (i) and 7x - y + 3 = 0 = angle between (i) and x + y - 3 = 0

$$\therefore \tan \theta = \frac{m-7}{1+7m} = \frac{m-(-1)}{1+m(-1)}$$

$$\Rightarrow$$
 m = -3 or 1/3

Hence possible equations of third side are y + 10 = -3(x-1)

and y + 10 =
$$\frac{1}{3}(x-1)$$

or
$$3x + y + 7 = 0$$
 and $x - 3y - 31 = 0$

(a)
 P₁ = length of perpendicular from (0,0) on x
 sec θ + y cosec θ = a

$$P_1 = \frac{a}{\sqrt{\sec^2 \theta + \csc^2 \theta}} = \frac{a}{\sqrt{\frac{1}{\cos^2 \theta} + \frac{1}{\sin^2 \theta}}}$$

= a sinθ .cosθ

or $2P_1 = a(2\sin\theta \cdot \cos\theta) \implies 2P_1 = a\sin 2\theta$

Similarly,
$$P_2 = \frac{a \cos 2\theta}{\sqrt{\cos^2 \theta + \sin^2 \theta}} = a \cos 2\theta$$

$$\therefore 4P_1^2 + P_2^2 = a^2 (\sin^2 2\theta \cdot \cos^2 2\theta) = a^2$$

7. (d

Let a and b are the intercepts on x and y-axes respectively.

$$a+b=9 \Rightarrow b=9-a....(i)$$

and the equation of the line is

$$\frac{x}{a} + \frac{y}{b} = 1$$
(ii)

From (i) and (ii)

$$\frac{x}{a} + \frac{y}{9-a} = 1$$
(iii)

this line also passes through the point (2,2)

: from (iii)
$$\frac{2}{a} + \frac{2}{9-a} = 1$$

On solving we get a = 6 or a = 3If a = 6 then b = 9 - 6 = 3

: equation of the line is
$$\frac{x}{6} + \frac{y}{3} = 1$$

or
$$x + 2y - 6 = 0$$

If $a = 3$ then $b = 9 - 3 = 6$

: equation of the line is
$$\frac{x}{3} + \frac{y}{6} = 1$$

or
$$2x + y - 6 = 0$$

Hence, required equation is

$$x + 2y - 6 = 0$$
 or $2x + y - 6 = 0$

Note: Solve this type of question with the help of given options.